'SIMPLE HARMONIC MOTION [S·H·M]'

|1|→ **Aperiodic motion** → A particle not Repet path in a same time interval.
* also called Non-periodic motion.

Eg → * A Bus or vehicle move in st. line
* Motion of Gas molecule.

|2|→ **Periodic Motion** → If particle Repet its path in a same time interval.

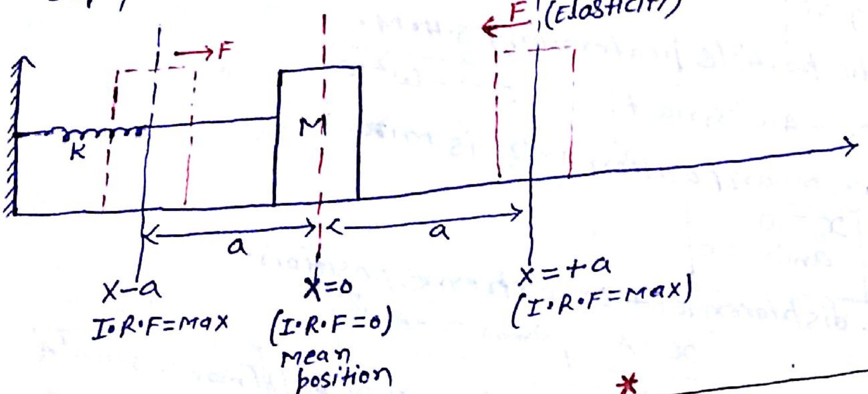
EX → * Motion of pendulum
* Motion around the nucleus
* Motion of planet around the sun.
* Motion of Earth w.r.t self axis.
* Motion of swift.
* Motion of liq in 'U' tube.
* Motion of Wooden plank at surface of liq.

|3|→ **Osscilatory/vibrational Motion** → If particle repet its path w.r.t same point & complete throw & flow motion in same time interval.

Eg → * Motion of pendulum
* Motion of swimmer
* Motion of liq in 'U' or 'V' tube.
* Motion of Medium particle when wave propagate in a medium.

AIIMS **NOTE** → All oscillating motion is periodic but all periodic motion is not osscilatory

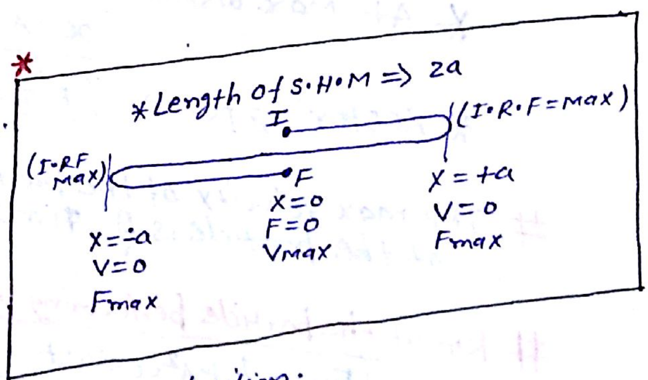
|4|→ **simple harmonic motion** → If a osscilatory motion is directelly propersnal to the disp. & always towards mean position.



$\boxed{F \propto -X}$

* $\boxed{F = -KX}$ — Disp. from mean position. / R.F coffiecient / opposite direction of force.

I.R.F ⇓ Elasticity



Exam * Disp. and distance in one osscilation Resp. zero & 4a.

Amplitude → Max disp. of medium particle from mean position.

NOTE → * Elasticity Inertia is necessory for oscillatory motion.
* S.H.M occur in stable eqm.
* General vibration of polyatomic gas molecule about its eqm position → S.H.M

Condition for S.H.M

$\boxed{F=-KX}$ $\boxed{A=-\omega^2 x}$ $\boxed{\frac{K}{M}=\omega^2}$ (ω = angular freq.)

$\boxed{\frac{d^2x}{dt^2}=-\omega^2 x}$ $\boxed{\frac{d^2x}{dt^2}+\omega^2 x=0}$ (Differential eqn of S.H.M)

Velocity of the particle performing S.H.M →

$\boxed{V=A\omega\sqrt{\frac{A^2-x^2}{A^2}}}$ $\boxed{V=\omega\sqrt{A^2-x^2}}$ $\boxed{V=\frac{2\pi}{T}\sqrt{A^2-x^2}}$

$\boxed{V=2\pi n\sqrt{A^2-x^2}}$

x = disp. of the particle from mean position.
T = Time period
A = Max disp. or, Amplitude.
ω = Angular freq
n = Linear freq.

Imp
* velocity of the particle at extreme position or at max disp. is equal to zero or, min.

$\boxed{x=A=90^\circ \quad V=\omega\sqrt{A^2-x^2} \quad V_{min}=0}$

* At mean position or, at an equilibrium position the velocity of the particle will be maximum.

$x=0$
$V=\omega\sqrt{A^2-0^2}$

$\boxed{V_{max}=A\omega=A(2\pi n)=A\times\left(\frac{2\pi}{T}\right)}$

* Averge velocity or, mean velocity

$\boxed{\vec{V}_{avg}=0}$

* Acc^n of the particle performing S.H.M.

$\boxed{a=-A\omega^2\sin\omega t}$ $\boxed{a=-\omega^2 x}$

* At eq^m or, mean position Acc^n is min

$\boxed{\begin{matrix}x=0\\ a_{min}=0\end{matrix}}$

* At max displacement or, extreme position.

$\boxed{x=A}$ $\boxed{a_{max}=-A\omega^2}$

* Restoring force $\boxed{F=ma}$, $\boxed{F=-m\omega^2 x}$, $\boxed{F_{max}=-m\omega^2 A}$

The max velocity of the particle performing S.H.M is 'α' & max Acc^n of the particle is β. Time period of oscillation → $\boxed{T=2\pi\left(\frac{\alpha}{\beta}\right)}$

K.E of the particle performing S.H.M →

$\boxed{\begin{matrix}E_K=\frac{1}{2}KA^2\cos^2\omega t\\ E_K=E_{Kmax}\cdot\cos^2\omega t\end{matrix}}$ $\boxed{K.E_{max}=\frac{1}{2}KA^2}$

Relation b/w K.E & disp →

$\boxed{E_K=\frac{1}{2}K(A^2-x^2)}$

* K.E of the particle is max at mean position or, equilibrium position → $\boxed{E_{Kmax}=\frac{1}{2}KA^2}$
* At max disp or, at extreme position

$\boxed{x=A}$ $\boxed{E_{Kmin}=0}$

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Avg. K.E or, Mean K.E →

$$\langle K.E \rangle = \frac{E_{Kmax} + E_{Kmin}}{2}$$

$$\langle K.E \rangle = \frac{\frac{1}{2}KA^2 + 0}{2}$$

$$\langle K.E \rangle = \frac{1}{4}KA^2$$

$$\langle K.E \rangle = \frac{1}{2} \times \underbrace{\frac{1}{2}KA^2}$$

$$\langle K.E \rangle = \frac{1}{2}E_{K max}$$

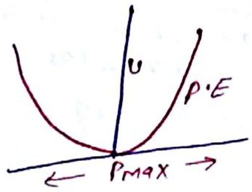
$$\langle K.E \rangle = \frac{K.E_{max} + K.E_{min}}{2}$$

$$\langle K.E \rangle = \frac{1}{?}KA^2$$

$$\boxed{\langle K.E \rangle = \frac{1}{2}K.E_{max}}$$

P.E of Particle performing S.H.M →

$\boxed{U = \frac{1}{2}Kx^2}$ $\boxed{H = \frac{1}{2}Kx^2}$



Avg. P.E or, Mean K.E ⇒

$$\langle P.E \rangle = \frac{U_{Kmax} + U_{Kmin}}{2}$$

$$\langle P.E \rangle = \frac{1}{2}U_{Kmax}$$

Relation b/w P.E & time →

$\boxed{U = \frac{1}{2}Kx^2}$

$\boxed{U = \frac{1}{2}KA^2 \sin^2 \omega t}$

Total energy of the particle performing S.H.M → Total E in S.H.M remain conserved it is equal to ~~sum~~ sum of K.E & P.E

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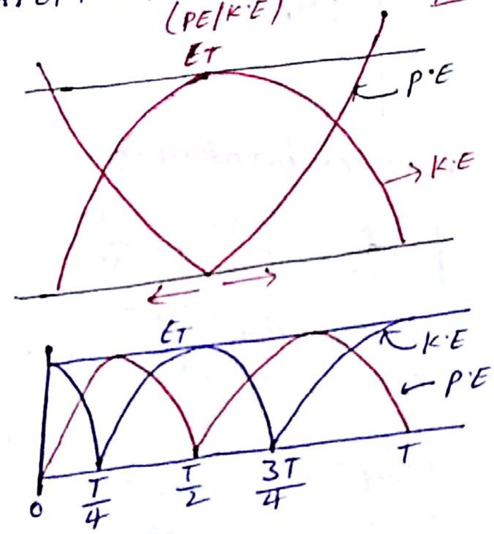
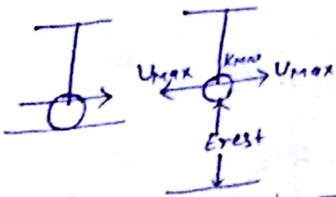
$$\boxed{\begin{aligned} E_T &= \frac{1}{2}KA^2 \\ E_T &= \frac{1}{2}m\omega^2A^2 \\ E_T &\propto m \\ E_T &\propto \omega^2 \propto n^2 \propto \frac{1}{T^2} \propto A^2 \\ E_T &\propto A^2 \end{aligned}}$$



NOTE → If Energy at rest is given in question.



* $\boxed{E_T = E_{rest} + U_{max}}$

* Fraction of P.E in T.E → $\frac{\frac{1}{2}kx^2}{\frac{1}{2}KA^2}$

* A particle having mass 'm' moving with a velo. 'v' strike from spring & compress it. cal. compression in spring → $\boxed{x = v\sqrt{\frac{m}{k}}}$

* A block is placed at a spring. If block is sepreated from the platform
Wich is performing S.H.M then the condn → $\omega^2 A = g$, $\frac{K}{m} A = g$

$$\boxed{E_T = K_{max} = U_{max} = \frac{1}{2} K A^2}$$

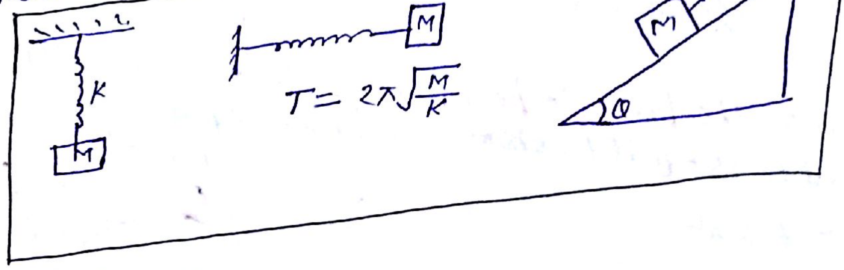
Spring pendulum

*$K = M\omega^2$
$\omega = \sqrt{\frac{K}{m}} = \sqrt{\frac{g}{x}}$

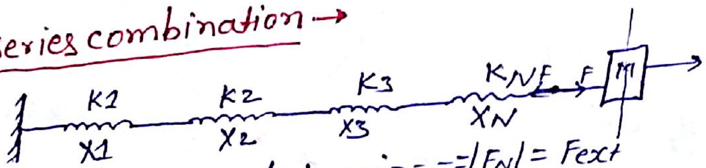
*$T = \frac{2\pi}{\omega} = 2\pi\sqrt{\frac{M}{K}} = 2\pi\sqrt{\frac{x}{g}}$.

Spring is used to store elastic P.E.

* When spring is compressed or, extended then work is done & this work is stored in the form elastic P.E.
* The force const. of a spring is inversally propersnal to the natural length.
* If a block of mass 'M' is suspended from a spring & it is slightly pulled & Released it will perform S.HM in this case Restoring force is ∝ to the disp.
* Time period of spring pendulum only depend on the Mass of suspended body & on force const. & it is independent from gravitation Accln. & extension in spring.
* In a freelly falling lift, at the centre of Earth & in artificial satellite time period of spring pendulum Remain unchange.



Series combination →



$|F_1| = |F_2| = |F_3| = \cdots = |F_N| = F_{ext}$

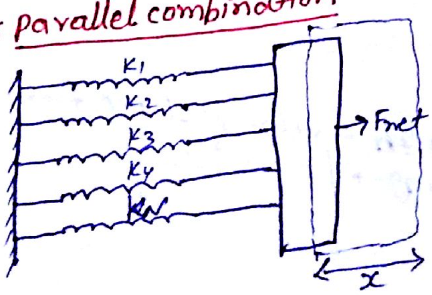
* $|F_1| = |F_2| = |F_3| \cdots\cdots X_N$
* $X = X_1 + X_2 + \cdots\cdots X_N$

$$\boxed{\frac{1}{K_{eq}} = \frac{1}{K_1} + \frac{1}{K_2} \cdots\cdots \frac{1}{K_N}}$$ (Spring const. of combination)

$T = 2\pi\sqrt{\frac{M}{K_{eq}}}$

$$\boxed{T = 2\pi\sqrt{M\left(\frac{1}{K_1} + \frac{1}{K_2} + \cdots \frac{1}{K_N}\right)}}$$ Time period of combination.

Parallel combination



$$\boxed{K_{eq} = K_1 + K_2 + K_3 \cdots K_N}$$

$T = 2\pi\sqrt{\frac{M}{K_{eq}}}$

$$\boxed{T = 2\pi\sqrt{\frac{M}{K_1 + K_2 + \cdots + K_N}}}$$

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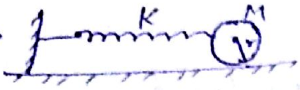
Standard Result for Spring :→

|a|→ 

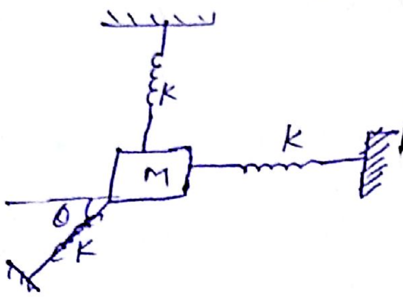
$\boxed{T = 2\pi\sqrt{\frac{\mu}{k}}}$ $\boxed{\mu = \frac{M_1 M_2}{M_1 + M_2}}$ μ = Reduce Mass.

|b|→ 

$\boxed{T = 2\pi\sqrt{\frac{M}{K}\left(1 + \frac{K_0^2}{r^2}\right)}}$ (k = spring const', k' = Radius of gyration)

|c|→ 

$\boxed{T = 2\pi\sqrt{\frac{M + m/3}{k}}}$

|d|→ 

$\boxed{T = \sqrt{\frac{M}{K(1-\cos^2\theta)}}}$

* Astronot use spring pendulum bcoz do not depend on G & L

Two different spring ossilate with same mass. It's time period Resp. T_1 & T_2 calculate time period of combination when—

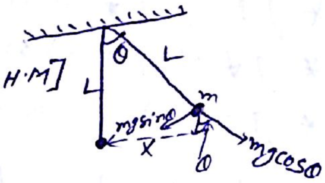
|i|→ It will connect in series & ossilate $\bar{c}$ same mean.

|ii|→ " " " " || " " " .

|i|→ $\boxed{T_{e\,series} = \sqrt{T_1^2 + T_2^2}}$ $\boxed{T_P T_S = T_1 T_2}$

|ii|→ $\boxed{T_{Parallel} = \frac{T_1 T_2}{\sqrt{T_1^2 + T_2^2}} = \frac{T_1 T_2}{T_S} \Rightarrow T_P T_S = T_1 T_2}$

SIMPLE PENDULUM



$F = -mg\sin\theta$

* $\theta \leq 5°$ (small) ⇒ SHM [$\theta > 5$ ⇒ ossilation not S.H.M]

$\boxed{F_R = -\left(\frac{mg}{L}\right)x}$

$\boxed{F = \frac{mg}{L} \Rightarrow \frac{m}{K} = \frac{L}{g}}$

$\boxed{T = 2\pi\sqrt{\frac{m}{K}} = 2\pi\sqrt{\frac{L}{g}}}$

NOTE → Time period of simple pendulum depend on length of pendulum & Gravitation Accl^n it is independent from mass of ossiclating body.

L = Length of pendulum ×

* If point mass osscilate = length of spring.
* If physical object is suspended = distance b/w point of suspension & centre of mass of osscilating body.

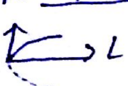
Effecting Factor :→

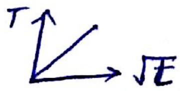
|a|→ Effect of Length → $T = 2\pi\sqrt{\frac{L}{g}}$

$g = const \Rightarrow T \propto \sqrt{L}$

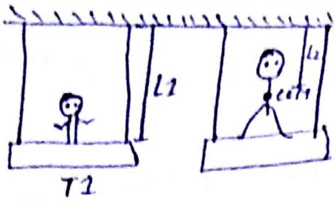
* $L\uparrow \Rightarrow T\uparrow \Rightarrow n\downarrow$ (slow)
* $L\downarrow \Rightarrow T\downarrow \Rightarrow n\uparrow$ (Fast)

Graph T v/s L→ * T v/s $\sqrt{L}$



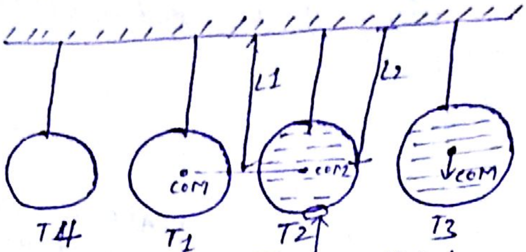


EX→
|i|→



$L_1 > L_2$
$T_1 > T_2$
$\boxed{n_1 > n_2}$

** Exemplar
|ii|→



$\boxed{L_1 = L_2 \quad T_1 = T_2}$ If a drill a hole.

* L First ↑ & then ↓
* T ~~first~~ First ↑ then ↓

$\boxed{T_3 > T_1 = T_2 = T_4}$

$\boxed{\begin{array}{l} * \text{change in 1 sec} = \frac{1}{2}\alpha\Delta T \\ * \text{change in 't' sec} = \left(\frac{1}{2}\alpha\Delta T\right) t \text{ sec} \\ * \text{change per day} = \left(\frac{1}{2}\alpha\Delta T\right) 86400 \frac{\text{sec}}{\text{day}} \\ * 1 \text{ yr} = \pi \times 10^7 \text{ sec} \end{array}}$

|b|→ **Effect of Gravity :→** $T = 2\pi\sqrt{\frac{L}{g}}$

* $L \Rightarrow$ same $\Rightarrow T = \frac{1}{\sqrt{g}}$
* $g\uparrow \Rightarrow T\downarrow \Rightarrow n\uparrow$ (Fast)
* $g\downarrow \Rightarrow T\uparrow \Rightarrow n\downarrow$ (slow)
* $g = 0 \Rightarrow T = \infty$ →
  - → At the centre of Earth.
  - → In a freely falling lift.
  - → In a Artificial satellite.

EX→ * At height above 'h' from Earth surface.
|i|→ $\boxed{T_s = 2\pi\sqrt{\frac{L}{g_s}}}$

$T_h = 2\pi\sqrt{\frac{L}{g_s/(1+h/R)^2}}$

$\boxed{T_h = T_s\,(1 + h/R)}$

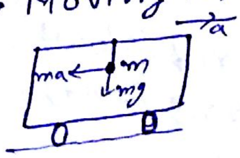
$\boxed{\%\ \text{change} = \frac{T_h - T_s}{T_s} = \frac{h}{R} \times 100\%}$

|ii|→ * At depth 'd' from earth surface →

$\boxed{g_d = g_s\left(1 - \frac{d}{R}\right)}$ $\boxed{T_d = \frac{T_s}{\sqrt{1 - d/R}}}$

* $\boxed{d\uparrow \Rightarrow g_d \Rightarrow T_d\uparrow \Rightarrow n\downarrow}$

|iii|→ * In a Moving ~~vehicle~~ vehicle
|a|→ Moving in a Horizontal plane.



$\boxed{g_{eff} = \sqrt{g^2 + a^2}}$

$\boxed{T = 2\pi\sqrt{\frac{L}{\sqrt{g^2 + a^2}}}}$

|b|→ Move in a circular path

$$\boxed{g_{eff} = \sqrt{g + \frac{V^4}{R^2}}} \qquad \boxed{T = 2\pi\sqrt{\frac{L}{\sqrt{g^2 + \frac{V^2}{R^2}}}}}$$

|c|→ Move in a incline plane

$$\boxed{T = 2\pi\sqrt{\frac{L}{g\cos\theta}}}$$

*** Ex→ In Moving Lift →

|a|→ Moving upward $\boxed{g_{eff} = g + a}$ $\boxed{T_{eff} = 2\pi\sqrt{\frac{L}{g+a}}}$

|b|→ Moving downward $\boxed{g_{eff} = g - a}$ $\boxed{T_{eff} = 2\pi\sqrt{\frac{L}{g-a}}}$

* If $V\uparrow$ (Accl^n) ⇒ $a = \oplus ve$
* If $V\downarrow$ (Retard) ⇒ $a = \ominus ve$

*** |c|→ Freely falling cond^n

$a = g \Rightarrow g_{eff} = g - g = 0$

$\boxed{T_{eff} = \infty}$

|d|→ If chain is break → Weightlessness cond^n

$\boxed{a = g}$

|e|→ If lift move with const Accl^n upward or, downward.

$\boxed{V = \text{const}}$ $\boxed{a = 0}$

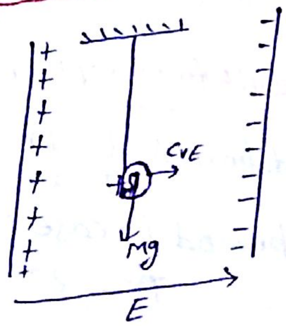
$\boxed{T = 2\pi\sqrt{\frac{L}{g}}}$

*** Ex→ osscilate in ⊕nce of Electric field →

|a|→ Horizontal electric Field

$$\boxed{g_{eff} = m\sqrt{g^2 + \left(\frac{qE}{m}\right)^2}}$$

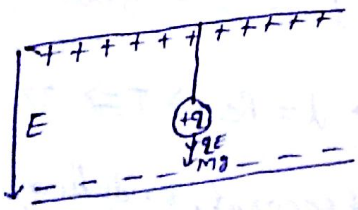
$$\boxed{T_{eff} = 2\pi\sqrt{\frac{L}{g^2 + \left(\frac{qE}{m}\right)^2}}}$$



|b|→ Downward eletric field

$$\boxed{g_{eff} = g + \frac{qE}{m}}$$

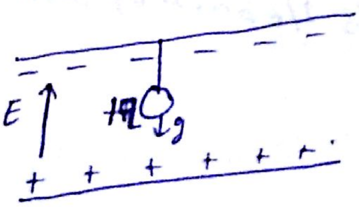
$$\boxed{T_{eff} = 2\pi\sqrt{\frac{L}{g + \frac{qE}{m}}}}$$



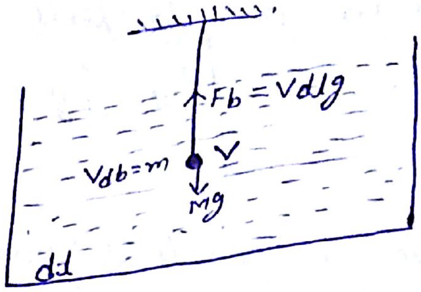
|c|→ upward Electric field.

$$\boxed{T = 2\pi\sqrt{\frac{l}{g - \frac{qE}{m}}}}$$

$$\boxed{g_{eff} = g - \frac{qE}{m}}$$



Ex→ In a non-viscous liq →



$$W_{eff} = mg\left(1 - \frac{d_l}{d_b}\right)$$

$$\boxed{g_{eff} = g(1 - d_l/d_b)}$$

$$T_{eff} = 2\pi\sqrt{\frac{L}{g(1 - d_l/d_b)}}$$

$$\boxed{T_L = \frac{T_{air}}{\sqrt{1 - \frac{d_l}{d_b}}}}$$

d_l → density of liq
d_b → density of body

* $\boxed{\text{Specific density} = \frac{d_{body}}{d_{H_2O}} = 6}$

$$\boxed{T_{H_2O} = \frac{T_{air}}{\sqrt{1 - \frac{1}{6}}}}$$

Two simple pendulum of time period T_1 & T_2 start vibrating at same phase then min time after which they are again in same phase ($T_1 > T_2$) → $\boxed{t = \frac{T_1 T_2}{T_1 - T_2}}$

* If $(n+1)$ → No. of osscilation completed by smaller pendulum then, (n) → Will be no. of oscillation completed by Larger pendulum. $\boxed{t = (n+1)T_2 = nT_1}$

Standard Result for simple pendulum :→

(a) → second pendulum ⇒ $L = 1m$ at surface of earth
$T = 2sec$ = const.

(b) → Time period in case of Long length pendulum.

$$T = 2\pi\sqrt{\frac{1}{g\left(\frac{1}{l} + \frac{1}{R_e}\right)}}$$

(i) → $l = \infty \Rightarrow T \Rightarrow \infty = 2\pi\sqrt{\frac{R_e}{g}}$ = 84.6 mit
= 1.414 hr
= $\sqrt{2}$ hr.

(ii) → $l = R_e \Rightarrow T \Rightarrow 2\pi\sqrt{\frac{R_e}{2g}} \Rightarrow \frac{84.6}{\sqrt{2}}$ mint $= 0.707 \times 84.6$ mint.

* Length of second pendulum at surface of Moon. Where gravitation Accln is 1/6 part of surface of Earth → $\boxed{L_m = \frac{L_e}{6} = 1/6\ m}$

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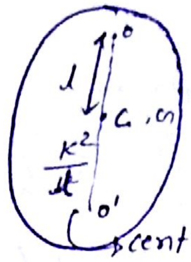
Compound pendulum

l = distance of suspension from centre of gyration (C.G)

r = Radius of gyration about C.G



$$\boxed{T = 2\pi\sqrt{\frac{I}{mgl}}}$$

$$\boxed{T = 2\pi\sqrt{\frac{l + \frac{k^2}{l}}{g}}}$$

If 'l' is Replaced by $\frac{k^2}{l}$

$\therefore$ then ($T \rightarrow$ same)

$\therefore$ T is same at distance $l + \frac{k^2}{l}$ from C.G

Linear S.H.M

(i) $\rightarrow$ $F = -Kx$

(ii) $\rightarrow$ $K = m\omega^2$

$T = 2\pi\sqrt{\frac{m}{K}}$

(iii) $\rightarrow$ $\frac{d^2x}{dt^2} + \omega^2 x = 0$

Angular S.H.M

(i) $\rightarrow$ $\tau = -C\theta$

(ii) $\rightarrow$ $C = I\omega^2$

$T = 2\pi\sqrt{\frac{I}{C}}$

(iii) $\rightarrow$ $\frac{d^2\theta}{dt^2} + \omega^2\theta = 0$

For small angle disp.

$\sin\theta \approx \theta$

$$\boxed{\tau = -(mgl)\theta}$$

$$\boxed{\tau = -C\theta}$$

$$\boxed{C = mgl}$$

I = M.O.I

m = mass of body

g = gravity

l = effective length.

Parallel axis theorum $\rightarrow$ $\boxed{I = I_{C.M} + Md^2}$

$\boxed{I_{CM} = MK'^2}$ K' = Radius of gyration

(a) $\rightarrow$ Ring $= I_{C.M} = MR^2 = MK^2 = \boxed{K' = R}$

(b) $\rightarrow$ Disc $= I_{C.M} = \frac{MR^2}{2} = MK'^2 \Rightarrow \boxed{K' = \frac{R}{\sqrt{2}}}$

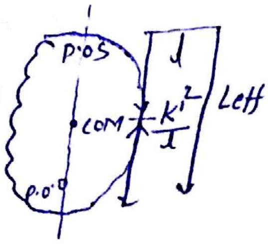
(c) $\rightarrow$ Solid sphere $I_{C.M} = \frac{2}{5}MR^2 = MK'^2 \Rightarrow \boxed{K' = \sqrt{\frac{2}{5}}R}$

(d) $\rightarrow$ Hollow Sphere $I_{C.M} = \frac{2}{3}MR^2 - MK'^2 = \boxed{K' = \sqrt{\frac{2}{3}}R}$

(e) $\rightarrow$ Rod $= I_{C.M} = \frac{ML^2}{12} = MK'^2 \Rightarrow \boxed{K' = \frac{L}{2\sqrt{3}}}$

$\boxed{T = 2\pi\sqrt{\frac{L_{eff}}{g}}}$ $\boxed{L_{eff} = \frac{K'^2}{l} + l}$

$T_{p.o.o} = T_{o.s}$



K'^2 = Radius of gyration.

Disc of Mass 'm' Radius 'R' suspended in a verticle w.r.t horizontal axis. calculate time period of its osscilation. when it is suspended From →

|i| → circumference.

$* \; K' = \frac{R}{\sqrt{2}} \Rightarrow \frac{K'}{l} = \frac{R^2/2}{R} = R/2$

$* \; L_{eff} = \frac{K'^2}{l} + l = \frac{3R}{2}$

$* \; T_{eff} = 2\pi\sqrt{\frac{L_{eff}}{g}} = 2\pi\sqrt{\frac{3R}{2g}}$

|ii| → At distance R/2 from COM

$* \; K' = \frac{R}{\sqrt{2}} = \frac{K'^2}{l} = \frac{(R/\sqrt{2})^2}{R/2} = R$

$* \; L_{eff} = \frac{K'^2}{l} + l = \frac{3R}{2}$

$* \; T = 2\pi\sqrt{\frac{3R}{2g}}$.

|iii| → At distance 3R/2 from circumference.

$l^2 - \left(\frac{T^2 g}{4\pi^2}\right) l + K'^2 = 0 \qquad \frac{T^2 g}{4\pi^2} = \frac{K'^2 + l^2}{l}$

* crossponding to same time period 4-points is possible.

|iv| → w.r.t COM

$l = 0 \qquad T = 2\pi\sqrt{\frac{L}{g}} = \infty$

$\frac{K'^2}{l} = \infty \qquad L_{eff} = \frac{K'^2}{l} + l = \infty$

NOTE → * If compound pendulum suspended from its C.O.M time period of pendulum is ∞ (max)

* When $K' = l$, time period of of pendulum is min.

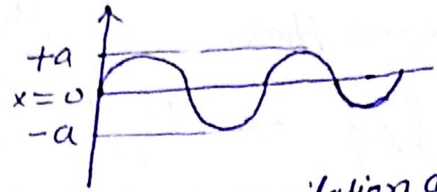
$$\boxed{T = 2\pi\sqrt{\frac{K'^2 + l}{g}}}$$

Scanned by CamScanner

Types of osscilation

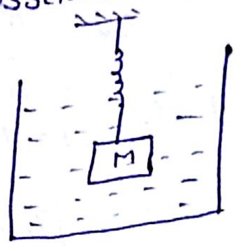
|a|→ Free osscilation → If amplitude, energy, time period of osscilation remain same.

$$\boxed{\frac{d^2x}{dt^2} + \omega^2 x = 0}$$



BCECE 2015

|b|→ Damped osscilation → If Amplitude of osscilation decrese with time.



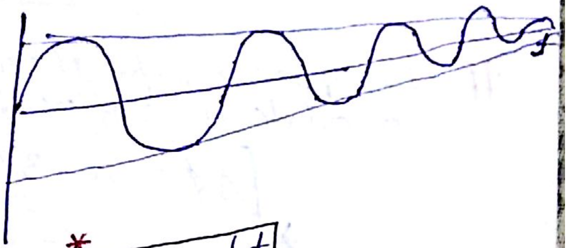
$F_R = -K_1 x$

** $\boxed{F_V = -6\pi\eta r v = -K_2 V}$ ← terminal velo.

viscous force

$F_{net} = -K_1 x - K_2 V$

* $\boxed{\frac{d^2x}{dt^2} + \left(\frac{K_2}{M}\right)\frac{dx}{dt} + \left(\frac{K_1}{M}\right)x = 0}$

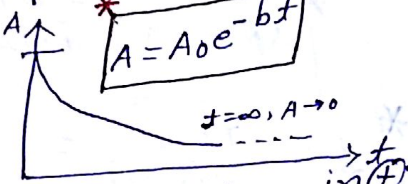


A_0 = Amplitude at $t=0$

b = damping cofficient

t = time

* $\boxed{A = A_0 e^{-bt}}$



NOTE → In damping osscilation Amplitude ↓ expontially w.r.t time.

|c|→ Forced osscilation → If free osscilation perform in ⊕ance of external periodic force.

$$\boxed{\frac{d^2x}{dt^2} + \left(\frac{K_2}{M}\right)\frac{dx}{dt} + \left(\frac{K_1}{M}\right)x = \frac{F_{ex}}{M}}$$

	ωt	$t\ (2\pi = T)$ AIPMT
# * $x=0$ to $x = A/2 = \frac{1}{2}$ or 30°	$\pi/6 = 30^\circ$	$T/12$
* $x=0$ to $x = \frac{A}{\sqrt{2}} = (\frac{1}{\sqrt{2}})$ or, 45°	$\pi/4$	$T/8$
* $x=0$ to $x = \sqrt{3}/2 = 60^\circ$	$\pi/3$	$T/6$
* $x=0$ to $x = A = 90^\circ$	$\pi/2$	$T/4$

A particle excicute S.H.M its velocity at position X_1 & X_2 Resp. V_1 & V_2 then Amplitude & time period →

$$\boxed{a = \sqrt{\frac{V_1^2 X_2^2 - V_2^2 X_1^2}{V_1^2 - V_2^2}}}$$

AIPMT 2015

$$\boxed{T = 2\pi\sqrt{\frac{X_2^2 - X_1^2}{V_1^2 - V_2^2}}}$$

Particle excicute S.H.M with amplitude 'a' calculate position of particle where, |i|→ $V = \frac{V_{max}}{2} \Rightarrow x = \pm\sqrt{\frac{3}{2}}a$

|ii|→ $V = \frac{\sqrt{3}}{2}V_{max} \Rightarrow x = \pm\frac{a}{2}$

Two particle exicute S.H.M with time period resp. T_1 & T_2 ($T_1 > T_2$). If Initially it will start with same phase calculate time after wich again it's come in a same phase.

$\boxed{\text{Same phase} = \text{even Multiple of } \pi}$

$\boxed{\Delta\phi = 2\pi\left(\frac{T_1 - T_2}{T_1 T_2}\right)t} = 0, 2\pi, 4\pi$

$\Delta\phi = 0, 2\pi, 4\pi, 6\pi ---- 2n\pi$

$$\boxed{t = 0, \frac{T_1 T_2}{T_1 - T_2}, \frac{2 T_1 T_2}{T_1 - T_2} ---- \frac{n T_1 T_2}{T_1 - T_2}}$$

$$\boxed{T_{min} = \frac{T_1 T_2}{T_1 - T_2}}$$

In upper concept If initially particle ~~at~~ in same phase calculate time after wich it come in opposite phase.

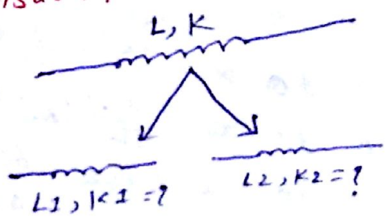
$\boxed{\Delta\phi = \pi, 3\pi, 5\pi ----- (2n-1)}$ $n = 1, 2, 3 ---$

* $\boxed{\Delta\phi = 2\pi\left(\frac{T_1 - T_2}{T_1 T_2}\right)t} = \pi, 3\pi, 5\pi --- (2n-1)\pi$

* $$\boxed{t = \frac{T_1 T_2}{2(T_1 - T_2)} = \frac{3 T_1 T_2}{2(T_1 - T_2)} = \frac{5 T_1 T_2}{2(T_1 - T_2)} --- \frac{(2n-1) T_1 T_2}{2(T_1 - T_2)}}$$

NOTE → * Time or position is not define Avg of K.E & P.E is $\frac{1}{4}ka^2$
* If freq of S.H.M is 'n' then freq of K.E & P.E is '2n'
* If freq. of S.H.M is 'n' then conversion ~~of~~ freq (kinetic to potential or, pot. to kinetic) is '4n'

A spring of spring const. 'k' devide into unequal part ratio of length is 1:n. Spring const. of indivisual part.



$\boxed{L_2 = nL_1}$

* $L_1 = \frac{L}{n+1} \Rightarrow K \propto \frac{1}{l}$

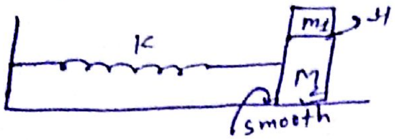
* $\frac{K_1}{K} = \frac{L}{l_1} = \frac{L}{\left(\frac{L}{n+1}\right)}$

$\boxed{K_1 = (n+1)K}$

* $L_2 = nL_1 = \frac{nL}{n+1} \Rightarrow K \propto \frac{1}{K} \Rightarrow \frac{K_2}{K} = \frac{L}{l_2} = \frac{L}{\frac{nL}{n+1}}$

$\boxed{K_2 = \frac{(n+1)}{n}K}$

Find max. amplitude of osscilation so that m1 does no leave on M2.



$$a\left(\frac{K}{m_1+m_2}\right) = \mu g$$

$$\boxed{a = \frac{\mu(M_1+m_2)g}{K}}$$

Max amplitude of osscilation so that block remain in contact.

during upward Accl$\underline{n}$

$$N_1 = m(g+a)$$

during down ward accl$\underline{n}$ $N_2 = m(g-a)$

If $N_2 > 0 \Rightarrow$ block Remain in contact.

$\boxed{g > a}$ → Accl$\underline{n}$

$\boxed{g > a\omega^2}$ → Amplitude

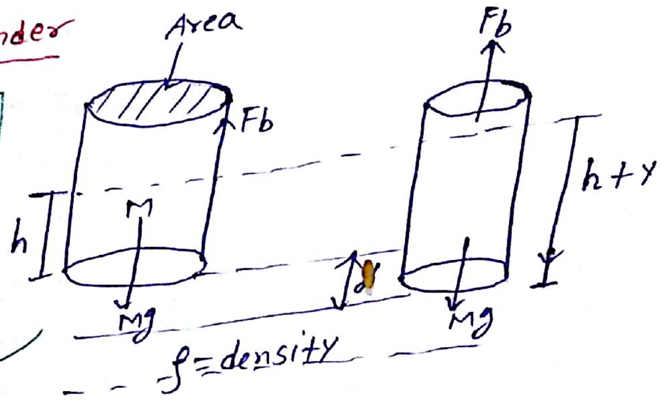
$$\boxed{a_{max} = \frac{mg}{K}}$$

2016 JIPMER

Time period of floating of cyllinder

$$\boxed{T = 2\pi\sqrt{\frac{h}{g}}} \quad (l=h)$$

Time period of liq in U-Tube.



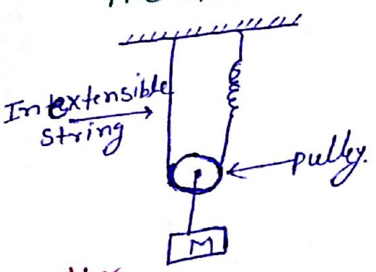
JIPMER 2016**

$$\boxed{T = 2\pi\sqrt{\frac{m}{A\rho g}}}$$

Motion of an oscillating liquid in u-tude → simple harmonic & time period Independent of density of liq.

**exemplar

Time period of mass 'M' when displaced from equilibrium position & then Released for the system shown in fig?



$$*\boxed{T = \frac{2\pi}{\omega} = \frac{2\pi}{\sqrt{\frac{4K}{M}}} = 2\pi\sqrt{\frac{M}{4K}}}$$

Exemplar

The length of second pendulum on the surface of Earth is 1m. then of second pendulum on the Moon? → $\boxed{1/6\ m}$